

ESERCIZI IN PIÙ**IL M.C.D. E IL m.c.m. FRA POLINOMI**

Determina M.C.D. e m.c.m. fra i seguenti polinomi.

1 $x^3 + 4x^2 - x - 4;$

$7x^3 - 7;$

$x^3 + 2x^2 + 2x + 1.$

[M.C.D. = 1; m.c.m. = $7(x - 1)(x + 1)(x + 4)(x^2 + x + 1)$]

2 $x^3 - 3x^2 - x + 3;$

$x^4 - 10x^2 + 9;$

$x^3 + x^2 - 5x + 3.$

[M.C.D. = $x - 1$; m.c.m. = $(x - 1)^2(x + 1)(x + 3)(x - 3)$]

3 $3x^2 + 10x - 8;$

$12x^2y - 8xy;$

$27x^4 - 54x^3 + 36x^2 - 8x.$

[M.C.D. = $3x - 2$; m.c.m. = $4xy(x + 4)(3x - 2)^3$]

4 $x^3 - 3x^2 + 4;$

$-8 + 8x - 2x^2;$

$x^3 - 2x^2 - x + 2.$

[M.C.D. = $x - 2$; m.c.m. = $2(x - 2)^2(x + 1)(x - 1)$]

5 $x^4 - 2a^2x^2 - 8a^4;$

$4a^2y^2 - x^2y^2;$

$x^3 - 8a^3.$

[M.C.D. = $x - 2a$; m.c.m. = $y^2(x - 2a)(x + 2a)(x^2 + 2a^2)(x^2 + 2ax + 4a^2)$]

6 $x^3 + 5x^2 - 9x - 45;$

$3x^3 + 3x^2 - 27x - 27;$

$2x^3 - x - 51.$

[M.C.D. = $x - 3$; m.c.m. = $3(x + 5)(x - 3)(x + 3)(x + 1)(2x^2 + 6x + 17)$]

7 $(2x - 3y)^2 - 9y^2;$

$2x^2 + 3y - x - 6xy;$

$2x^2 + 7x - 4.$

[M.C.D. = 1; m.c.m. = $4x(x - 3y)(2x - 1)(x + 4)$]

8 $x^2 - 4x + 4 + 3xy - 6y;$

$2x^3 - 16;$

$x^3 - 3x^2 + 4.$

[M.C.D. = $x - 2$; m.c.m. = $2(x - 2)^2(x + 1)(x - 2 + 3y)(x^2 + 2x + 4)$]

9 $(a - 3b)^2 - 9x^2;$

$a^2 - 3x^2 - 3bx - 3ab - 2ax;$

$-4ax^2 + 2a^2x - 6bx^2 - 6abx - 6x^3.$

[M.C.D. = $a - 3b - 3x$; m.c.m. = $2x(x + a)(a - 3b - 3x)(a - 3b + 3x)$]

10 $x^6 + 7x^3 - 8;$

$x^2 + x - 2;$

$x^4 - x^3 + 3x^2 + 2x + 4.$

[M.C.D. = 1; m.c.m. = $(x - 1)(x + 2)(x^2 + x + 1)(x^2 - 2x + 4)$]