

**YOU & MATHS** **Possible values** Could the fraction  $\frac{3}{x-2}$  take on the value  $\frac{3}{2}$  (that is, can  $\frac{3}{x-2} = \frac{3}{2}$ )?

For what value of  $x$ ? Give another example of a value it can take on and an example of a value it cannot take on.

The fraction exists only if  $x \neq 2$ ; so  $x - 2$  is not 0, and to solve  $\frac{3}{x-2} = \frac{3}{2}$  you can multiply both sides of the equation by  $2(x - 2)$ , which gives  $3 \cdot 2 = (x - 2) \cdot 3$ .

This is equivalent to

$$3x - 6 = 6.$$

So  $3x = 12$ , and  $x = 4$ , which is an acceptable value.

To find an example of another value that the fraction  $\frac{3}{x-2}$  can take on, we can proceed by trials.

Let  $\frac{3}{x-2}$  be equal to 6. Then

$$\frac{3}{x-2} = 6 \rightarrow 3 = 6(x - 2) \text{ for } x \neq 2.$$

This is equivalent to

$$3 = 6x - 12 \rightarrow 6x = -15 \rightarrow x = -\frac{15}{6},$$

which is an acceptable value.

The only time when we will not be able to find a value that  $\frac{3}{x-2}$  can take on is when the solution of the equation is not an acceptable value, i.e. when  $x = 2$ .